


Multiplication Methods

Partial Products

You can use place-value to multiply. Find the product for 3×14 .

What You Show	What You Write
 <p> $3 \times 10 = 30$ $3 \times 4 = 12$ $30 + 12 = 42$ </p>	$\begin{array}{r} 14 \\ \times 3 \\ \hline 12 \\ + 30 \\ \hline 42 \end{array}$ <p> 3×4 ones 3×1 ten </p>

Open Array

You can use an open array to multiply. Find the product for 3×14 .

	10	+	4	
3	(3 x 10) 30	(3 x 4) 12		$\begin{array}{r} 30 \\ + 12 \\ \hline 42 \end{array}$

These methods can be applied to multi-digit numbers.

Open Array:

	40	+	2	
30	(30 x 40) 1200	(30 x 2) 60		1200 60 40
+	(1 x 40) 40	(1 x 2) 2		$\begin{array}{r} + 2 \\ \hline \mathbf{1302} \end{array}$
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Partial Products:

$$\begin{array}{r} 42 \\ \times 31 \\ \hline 2 \text{ (1 x 2)} \\ 40 \text{ (1 x 40)} \\ 60 \text{ (30 x 2)} \\ \underline{1200 \text{ (30 x 40)}} \\ \mathbf{1302} \end{array}$$

Division Methods

Ladder or Forgiving Method

The ladder method allows students to think about division by using factors that are easy for them to work with, such as tens or multiples of tens. Students' work using this method may vary, but they can efficiently get the same answer as the traditional algorithm. Here are two examples:

$$\begin{array}{r|l} 276 & \\ 3 \overline{) 828} & \\ \hline - 600 & 200 \times 3 \\ \hline 228 & \\ - 210 & 70 \times 3 \\ \hline 18 & \\ - 18 & 6 \times 3 \\ \hline 0 & 276 \end{array}$$

$$\begin{array}{r|l} 3 \overline{) 828} & 100+100+50+20+6=276 \\ \hline -300 & 100 \times 3 \\ \hline 528 & \\ -300 & 100 \times 3 \\ \hline 228 & \\ -150 & 50 \times 3 \\ \hline 78 & \\ -60 & 20 \times 3 \\ \hline 18 & \\ -18 & 6 \times 3 \\ \hline 0 & \end{array}$$

Column Division

By dividing the problem into place-value columns, you can do a series of smaller division problems to find the answer.

$$\begin{array}{r|c|c} 1 & 3 & 6 \\ 5 \overline{) 6} & \cancel{8} & \cancel{3} \\ \hline -5 & 18 & 33 \\ \hline \cancel{1} & -15 & -30 \\ \hline & \cancel{3} & 3 \end{array}$$

Multiplying Up

You can divide by thinking of the related multiplication fact. For example, $270 \div 18 = ?$ can be thought of as $18 \times ? = 270$. You can multiply up until you get to 270.

$10 \times 18 = 180$ and $20 \times 18 = 360$, so the answer is between 10 and 20

$$5 \times 18 = 90$$

$$90 + 180 = 270$$

so $18 \times 15 = 270$ and $270 \div 18 = 15$

Here is an array model showing this method:

	18	
10	$10 \times 18 = 180$	$\begin{array}{r} 180 \\ +90 \\ \hline 270 \end{array}$
5	$5 \times 18 = 90$	